



cuit of the HEMT we use for our investigations. The linear and not bias dependent extrinsic elements  $L_g$ ,  $L_{db}$ ,  $L_s$  and  $R_g$ ,  $R_{db}$ ,  $R_s$  are extracted from small signal S-parameter measurements using hot and cold modeling techniques. To determine the nonlinear elements of the inner transistor ( $R_{gs}$ ,  $R_{gd}$ ,  $C_{gs}$ ,  $C_{gd}$ ,  $C_{ds}$ ,  $G_m$ ,  $G_{ds}$ ,  $\tau$ ) we apply a deembedding procedure to the measured small signal S-parameter data of 200 different bias points [1,2]. This has to be done for all interesting frequencies. The nonlinear elements can be modeled either by analytical functions or by interpolation using look-up-tables [3]. The two dimensional look-up-tables contain the data of the nonlinear elements as function of the two independent controlling voltages  $V_{gs}$  and  $V_{ds}$  at the intrinsic HFET. Both approaches are based on a quasistatic approximation. The nonlinear diode admittances  $G_{gs}$  and  $G_{gd}$  are given by their I/V-characteristics whereas the parameters have been determined by DC measurements. To model the channel current  $I_{ds}$  we use the DC I/V-characteristic (Fig. 2) and the dynamic output I/V characteristic we get by an integration of the differential small signal RF admittances  $G_m$  and  $G_{ds}$  (Fig. 3). So dispersion effects of  $G_{ds}$  are included.

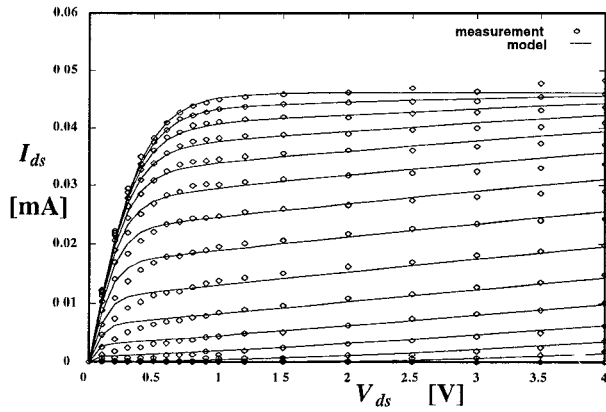


Fig. 2 DC characteristic  $I_{ds} = f(U_{ds})$

## Discussion of the noise sources

The high frequency noise performance of the HFET is described by the model given in [4,5] which uses three uncorrelated white noise current sources ( $I_{Nds}$ ,  $I_{NRgs}$ ,  $I_{NRgd}$ ) allocated to the resistive elements of the intrinsic transistor. The parameters of these noise sources are determined from noise parameter measurements using the correlation matrix method. Baseband noise

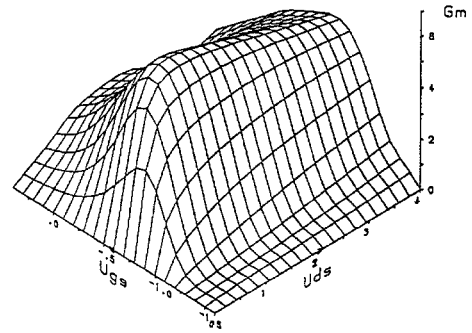


Fig. 3a Transconductance  $G_m = \left. \frac{\partial I_{ds}}{\partial U_{gs}} \right|_{\partial U_{ds}=0}$

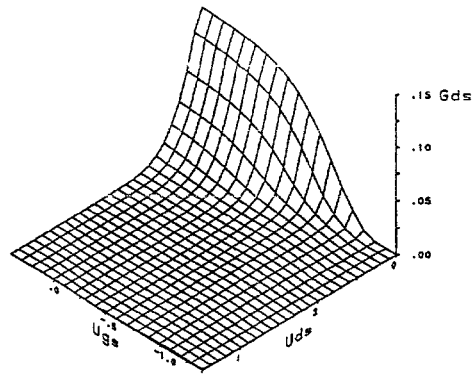


Fig. 3b Output admittance  $G_{ds} = \left. \frac{\partial I_{ds}}{\partial U_{ds}} \right|_{\partial U_{gs}=0}$

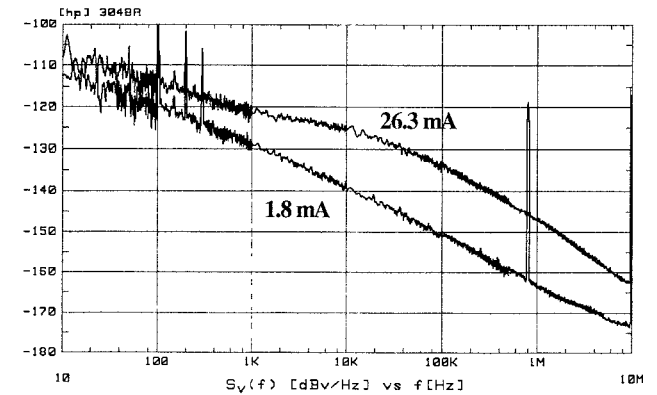


Fig. 4 Measured baseband noise of an AlGaAs/GaAs-HEMT showing  $f^{-a}$  - and  $g-r$  noise at different bias points

measurements were done to determine the bias dependent low frequency noise power spectra (Fig. 4). The low frequency noise contribution is modeled as a noise current source  $I_{NF}$ , which includes the fundamental  $f^{-a}$  noise source and the  $g-r$  noise source showing an Lorentzian spectrum [6]. Besides of the

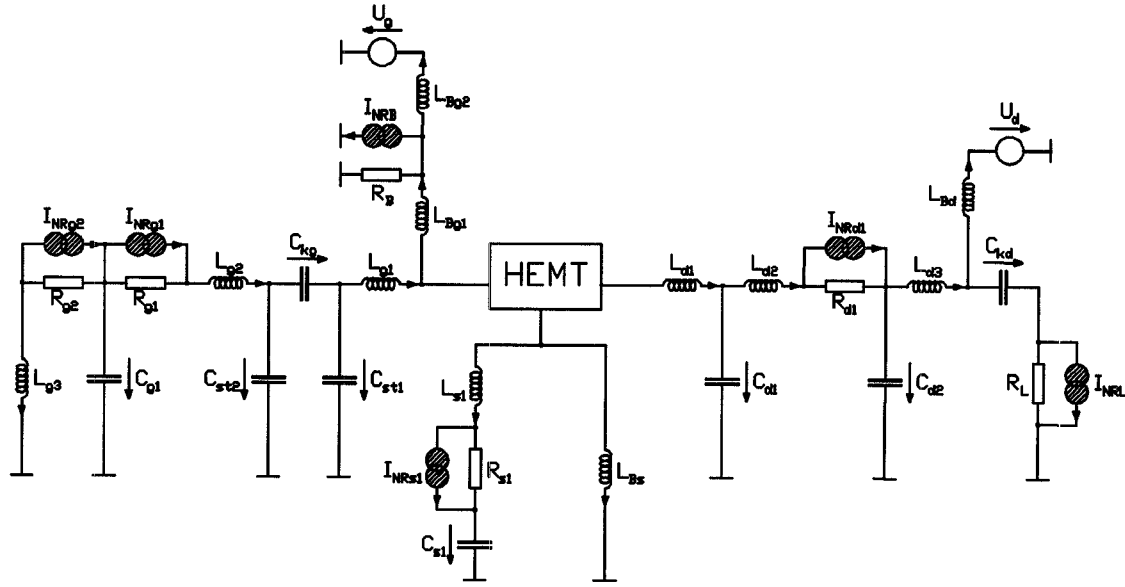


Fig. 5 Lumped element equivalent circuit of the HEMT oscillator

three white noise current sources  $I_{Nds}$ ,  $I_{NRgs}$  and  $I_{NRgd}$  in the intrinsic HEMT the large signal and noise model also includes noise sources for the shot noise of the Schottky diodes ( $I_{Ngs}$ ,  $I_{Ngd}$ ) and the thermal noise of the parasitic resistances ( $R_g$ ,  $R_d$ ,  $R_s$ ). The noise source  $I_{Nds}$  describes the diffusion noise of the channel current  $I_{ds}$  (hot electrons).

In general the diffusion noise of the channel current dominates all other noise contributions. Usually the Schottky noise of the diodes can be neglected. This is not applicable if the diodes show high leakage currents. The Nyquist noise of the resistances is responsible for the minimum noise figure of the HEMT and we have to take it into consideration.

## Design of the oscillator

The modeling process was performed on a standard AlGaAs/GaAs-HEMT CFY65. The oscillator is fabricated as hybrid circuit on  $Al_2O_3$ -substrate using coplanar lines. The design is done using the reflection coefficient method. The oscillation frequency is determined by a short circuited coplanar resonator connected to the gate of the HEMT. Two parallel coplanar lines provide a capacitive load to the source of the transistor and cause the instability for oscillation. The oscillator power is coupled out at the drain of the HEMT.

## Phase noise calculation

For the application of the time domain phase noise simulation (TDPNS) method [6,7,8], the oscillator circuit is approximated by a lumped element circuit model (Fig. 5). The lines connected to gate and source of the HEMT are also modeled with lumped elements. This is due to the fact that the calculation method we apply is done in time domain. The Langevin equations - a set of ordinary first order nonlinear differential equations - describe the deterministic and stochastic behavior of the oscillator. A perturbation formulation allows the consideration of the noise contributions. As a result of the calculation we get the phase noise spectrum  $L(f_m)$  of the oscillator given by

$$L(f_m) = \frac{\Delta f_{3dB}}{\pi \cdot f_m^2} \quad \text{white noise} \\ + \sum_{k=1}^K |g_{1,0}^k|^2 \frac{\omega_0^2 c_k}{|2\pi f_m|^{2+\alpha}} f^{-\alpha} \quad \text{noise } (1 < \alpha < 2) \\ + \sum_{i=1}^I |r_{1,0}^i|^2 \frac{\omega_0^2}{|2\pi f_m|^2} \frac{\alpha_{gr}}{1 + (f_m \tau_{gr})^2} \quad \text{g-r noise}$$

While the first term results from the white noise sources in the circuit, the second and the third term are caused by low frequency  $f^{-\alpha}$  and g-r noise contri-

butions. In Fig. 6 and Fig. 7 this different contributions are separately displayed and compared with the measured oscillator phase noise. Evaluating the result we can find that up to 10 kHz the phase noise of the oscillator is dominated by the  $1/f$  noise behavior of the active element corresponding to a slope of 30dB/decade. In the offset frequency range 10 kHz to 8 MHz the phase noise is determined by the  $g$ - $r$  noise contribution and above 8 MHz the white noise sources will dominate the phase noise behavior.

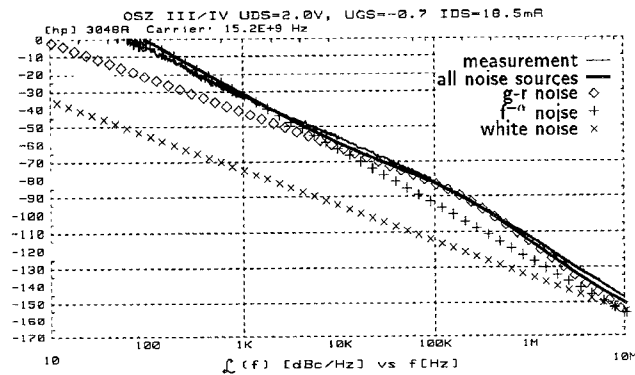


Fig. 6 Measured and calculated phase noise performance of the coplanar HEMT oscillator

## Conclusion

In general we find that the phase noise of this oscillator with -30dBc/Hz at an offset frequency of 1 kHz is very high. This is first due to the fact that the

	$L(f_m)$ [dBc/Hz]
$R_{q2}$	-158.7
$I_{Nds}$	-159.2
$R_L$	-164.6
$R_{g1}$	-165.7
$R_v$	-167.6
$R_{gd}$	-167.8
$R_g$	-168.4
$R_B$	-168.7
$R_{gs}$	-170.2
$R_d$	-175.0
$R_{s1}$	-179.0
$R_{d1}$	-183.5
$I_{Ngd}$	-246.4
$I_{Ngs}$	-249.2
<b>Summe</b>	<b>-154.2</b>

Fig. 7 Contribution of the different noise sources to the phase noise at  $f_m = 10$  MHz

HEMT element shows very high  $f^{-a}$  noise. Another reason lies in the loaded Q factor of the coplanar resonator which is in the order of 10 and very low. The analysis shows in a clear manner how the different noise sources contribute to the over all noise behavior of the oscillator.

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